

# Package: RRMLRfMC (via r-universe)

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**Type** Package

**Title** Reduced-Rank Multinomial Logistic Regression for Markov Chains

**Version** 0.4.0

**Description** Fit the reduced-rank multinomial logistic regression model for Markov chains developed by Wang, Abner, Fardo, Schmitt, Jicha, Eldik and Kryscio (2021)<[doi:10.1002/sim.8923](https://doi.org/10.1002/sim.8923)> in R. It combines the ideas of multinomial logistic regression in Markov chains and reduced-rank. It is very useful in a study where multi-states model is assumed and each transition among the states is controlled by a series of covariates. The key advantage is to reduce the number of parameters to be estimated. The final coefficients for all the covariates and the p-values for the interested covariates will be reported. The p-values for the whole coefficient matrix can be calculated by two bootstrap methods.

**License** GPL-2

**Encoding** UTF-8

**LazyData** true

**Imports** nnet

**Depends** R (>= 3.5.0)

**RoxygenNote** 7.1.1

**Suggests** rmarkdown, knitr

**NeedsCompilation** no

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**Repository** <https://wangp33.r-universe.dev>

**RemoteUrl** <https://github.com/cran/RRMLRfMC>

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Aupdate	<i>Aupdate</i>
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### Description

This function is used to update A matrix

### Usage

Aupdate(Dfix, Gamma, Adata, R, p, q, I, iniA, eps, refA)

### Arguments

Dfix	the coefficient matrix for study covariates
Gamma	the G matrix value
Adata	the dataset
R	the rank of reduced rank model
p	the number of covariates in the dimension reduction
q	the numbne of study covariates
I	a U by U incidence matrix with elements; I(i,j)=1 if state j can be accessed from state i in one step and 0 otherwise
iniA	initial value for the iteration
eps	the tolerance for convergence, default is 10 <sup>-5</sup>
refA	a vector of reference categories

### Value

a list of outputs:

- NewA: the updated A matrix
- loglikeA: the loglikelihood when updating A

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cogdat	<i>Cognitive Dataset</i>
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### Description

A dataset containing the states and covariates of 649 participants enrolled in the BRAiNS cohort at the University of Kentucky's Alzheimer's Disease Research Center.

### Usage

cogdat

### Format

A data frame with 6240 rows and 14 columns:

**ID** used to denote the participants; from 1 to 649

**visitno** used to denote the visit number for each participant

**prstate** denote the previous state

**custate** denote the current state

**bagec** baseline age (centered at age 72)

**famhx** family history of dementia

**HBP** self reported high blood pressure

**apoe4** at least one Apolipoprotein-E (APOE) gene  $\epsilon$ 4 allele

**smk1** cigarette smoking level (none versus < 10)

**smk2** cigarette smoking level (11-19)

**smk2** cigarette smoking level ( $\geq$  20 pack years))

**lowed** low education

**headinj** self reported head injury

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derivativeB	<i>derivativeB</i>
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### Description

This function is used to calculate the loglikelihood with a given matrix  $B=AG$

### Usage

derivativeB(B, I, zy, refd)

**Arguments**

B	a numeric coefficient matrix
I	U by U incidence matrix with elements; $I(i,j)=1$ if state j can be accessed from state i in one step and 0 otherwise
zy	the variable values for a given observation
refd	a vector of reference categories

**Value**

loglikelihood

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derivatives

*derivatives*

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**Description**

This function is used calculate the derivative values (first and second derivatives for Newton-Raphson method) and loglikelihood when updating A

**Usage**

```
derivatives(A, Gamma, Dmat, I, zy, refA)
```

**Arguments**

A	matrix with value from previous iteration
Gamma	G matrix values
Dmat	the coefficient matrix for the fixed variables,
I	a U by U incidence matrix with elements; $I(i,j)=1$ if state j can be accessed from state i in one step and 0 otherwise
zy	the variable values for a given observation
refA	a vector of reference categories

**Value**

a list of outputs:

- fird: the first derivative value
- secd: the second derivative value
- loglike: the loglikelihood

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expand	<i>expand</i>
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**Description**

This function is used to expand the Y(category) to a indicator vector

**Usage**

```
expand(pri, curr, I, refE)
```

**Arguments**

pri	the prior state
curr	the current state
I	a U by U incidence matrix with elements; $I(i,j)=1$ if state j can be accessed from state i in one step and 0 otherwise
refE	a vector with the reference categories

**Value**

ry: a indicator vector

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Gupdate	<i>Gupdate</i>
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**Description**

This function is used to update G matrix

**Usage**

```
Gupdate(A, Gdata, p, q, I, refG)
```

**Arguments**

A	numeric matrix
Gdata	the dataset used to update G
p	the number of covariates in the dimension reduction
q	the numbne of study covariates
I	a U by U incidence matrix with elements; $I(i,j)=1$ if state j can be accessed from state i in one step and 0 otherwise
refG	a vector of reference categories

**Value**

a list of outputs:

- NewG: the updated G matrix
- loglikeK: the loglikelihood when updating G
- sderr: standard errors for the coefficient matrix

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norm

*norm*

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**Description**

This function is used to normalize a vector to have unit length

**Usage**

norm(x)

**Arguments**

x                    a numeric vector

**Value**

a normalized vector with length 1

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rrmultinom

*rrmultinom*

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**Description**

This function is used to fit the reduced rank multinomial logistic regression for markov chain

**Usage**

rrmultinom(I, z1 = NULL, z2 = NULL, T, R, eps = 1e-05, ref = NULL)

**Arguments**

I	a U by U incidence matrix with elements; U is number of states; I(i,j)=1 if state j can be accessed from state i in one step and 0 otherwise
z1	a n by p matrix with covariates involved in the dimension reduction(DR), n is the number of subjects, p is the number of covariates involved in DR
z2	a n by q matrix with study covariates (not in dimension reduction), q is the number of study covariates
T	a M by 3 state matrix, <ul style="list-style-type: none"> <li>• the first column is a subject number between 1,...,n;</li> <li>• the second column is time;</li> <li>• the third column is the state occupied by subject in column 1 at time indicated in column 2</li> </ul>
R	the rank
eps	the tolerance for convergence; the default is $10^{-5}$
ref	a vector of reference categories; the default is NULL and if NULL is used, the function will use the first category as the reference category for each row

**Value**

a list of outputs:

- Alpha: the final A matrix
- Gamma: the final G matrix
- Beta: the coefficient matrix for variables involved in reduced rank
- Dcoe: the coefficient matrix for the fixed variables
- Dsderr: the standard error matrix for the fixed variables
- Dpval: the p-value matrix for the fixed variables
- coemat: the overall coefficient matrix
- niter: the iteration number to get converged
- df: the degrees of freedom
- loglik: the final loglikelihood
- converge: three possible values with 0 means fail to converge, 1 means converges, and 2 means the maximum iteration is achieved

**Examples**

```
# generate the Markov chain
U=7
I1=I2=I3=rep(1,7)
I4=c(0,0,0,1,1,1,1)
I5=I6=I7=rep(0,7)
I=rbind(I1,I2,I3,I4,I5,I6,I7)
# prepare the data
data=cogdat
```

```

n=length(unique(data[,1]))
M=nrow(data)+n
Mc=0
z=matrix(0,n,9)
colnames(z)=colnames(data)[5:13]
T=matrix(0,M,3)
for(i in 1:n){
  subdat=data[which(data[,1]==i),,drop=FALSE]
  z[i,]=subdat[1,5:13]
  mc=nrow(subdat)
  T[(Mc+1):(Mc+mc+1),1]=i
  T[(Mc+1):(Mc+mc+1),2]=0:mc
  T[(Mc+1):(Mc+mc+1),3]=c(subdat[1,3],subdat[,4])
  Mc=Mc+mc+1
}
#z1=z[,c(1:3),drop=FALSE]
z2=z[,4,drop=FALSE]
# fit the model with rank 1
rrmultinom(I,z1=NULL,z2,T,1,eps=9,ref=c(1,1,1,4))

```

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sdfun

*sdfun*


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## Description

This function is used get the standard error matrix from bootstrap method It returns the matrices of standard error and p-value for the coefficient matrix

## Usage

```
sdfun(I, z1 = NULL, z2 = NULL, T, R, eps = 1e-05, B, tpoint = NULL, ref)
```

## Arguments

I	a U by U incidence matrix with elements; U is the number of states; I(i,j)=1 if state j can be accessed from state i in one step and 0 otherwise
z1	a n by p matrix with covariates involved in the dimension reduction(DR), n is the number of subjects, p is the number of covariates involved in DR
z2	a n by q matrix with study covariates (not in dimension reduction), q is the number of study covariates
T	a M by 3 state matrix, <ul style="list-style-type: none"> <li>• the first column is a subject number between 1,...,n;</li> <li>• the second column is time;</li> <li>• the third column is the state occupied by subject in column 1 at time indicated in column 2</li> </ul>
R	the rank



eps	the tolerance for convergence; the default is $10^{-5}$
B	the bootstrap number
tpoint	a matrix has two columns with the participants' visit information about timeline
ref	a vector of reference categories

### Value

a list of outputs:

- coe: the coefficient matrix of the original data
- sd: the standard error matrix
- pvalue: the p-value matrix

### Examples

```
# generate the Markov chain
U=7
I1=I2=I3=rep(1,7)
I4=c(0,0,0,1,1,1,1)
I5=I6=I7=rep(0,7)
I=rbind(I1,I2,I3,I4,I5,I6,I7)
# prepare the data
data=cogdat
n=length(unique(data[,1]))
M=nrow(data)+n
Mc=0
z=matrix(0,n,9)
colnames(z)=colnames(data)[5:13]
T=matrix(0,M,3)
for(i in 1:n){
  subdat=data[which(data[,1]==i),,drop=FALSE]
  z[i,]=subdat[1,5:13]
  mc=nrow(subdat)
  T[(Mc+1):(Mc+mc+1),1]=i
  T[(Mc+1):(Mc+mc+1),2]=0:mc
  T[(Mc+1):(Mc+mc+1),3]=c(subdat[1,3],subdat[,4])
  Mc=Mc+mc+1
}
#z1=z[,c(1:3),drop=FALSE]
z2=z[,4,drop=FALSE]
# find the standard deviation matrix for the model with rank 1
sdfun(I,z1=NULL,z2,T,1,eps = 9,2,ref=c(1,1,1,4))
```

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